

WEIGHTED ARITHMETIC MEAN.

We provide equal weightage to every individuals when calculating ^{simple} arithmetic mean.

But really there are own different importance of every individuals in series.

Weighted arithmetic mean provide their own value and calculate mean.

* Direct method of calculation of weighted Arithmetic mean -

$$\bar{X}_w = \frac{\sum W \cdot X}{\sum W}$$

Where,

\bar{X}_w = Weighted arithmetic mean.

$\sum W \cdot X$ = Sum of weight \times individual value.

$\sum W$ = Sum of weight.

* Short cut method -

$$\bar{X}_w = A_w + \frac{\sum W \cdot dx}{\sum W}$$

Where,

A_w = Assumed weighted mean.

dx = X - Assumed weighted mean.

Ex Computed the weighted arithmetic mean of the index number from the following data -

Group	INDEX No.	Weight
Food	125	10
clothing	130	8
Fuel and light	140	6
House rent	170	2
Miscellaneous	180	4

Solution.

Group	Index No.	Weight (w)	Direct method $w \times x$	INDirect method dx / x = 140	w dx.
Food	125	10	1250	-15	-150
clothing	130	8	1040	-10	-80
Fuel and light	140	6	840	0	0
House rent	170	2	340	30	60
Miscellaneous	180	4	720	40	160
		$\Sigma w = 30$	$\Sigma wx = 4190$		$\Sigma wx = 10$

Direct method

$$\begin{aligned} \bar{X}_w &= \frac{\Sigma wx}{\Sigma w} \\ &= \frac{4190}{30} \\ &= 139.67 \end{aligned}$$

Weighted mean (short cut method)

$$\begin{aligned} \bar{X}_w &= A + \frac{\Sigma dx}{\Sigma f} \\ &= 140 + \frac{10}{30} \\ &= 140 + 0.33 \\ &= 139.7 \end{aligned}$$